



STABILITY CALCULATIONS WITH SAND BALLAST

Scenario 1: Two stacked sand-filled T1 TYPAR GEOCELLS units:

A free-body diagram of the forces acting on the Scenario 1 arrangement is shown in Figure 1.0 below. The cells are analyzed as a monolithic system.

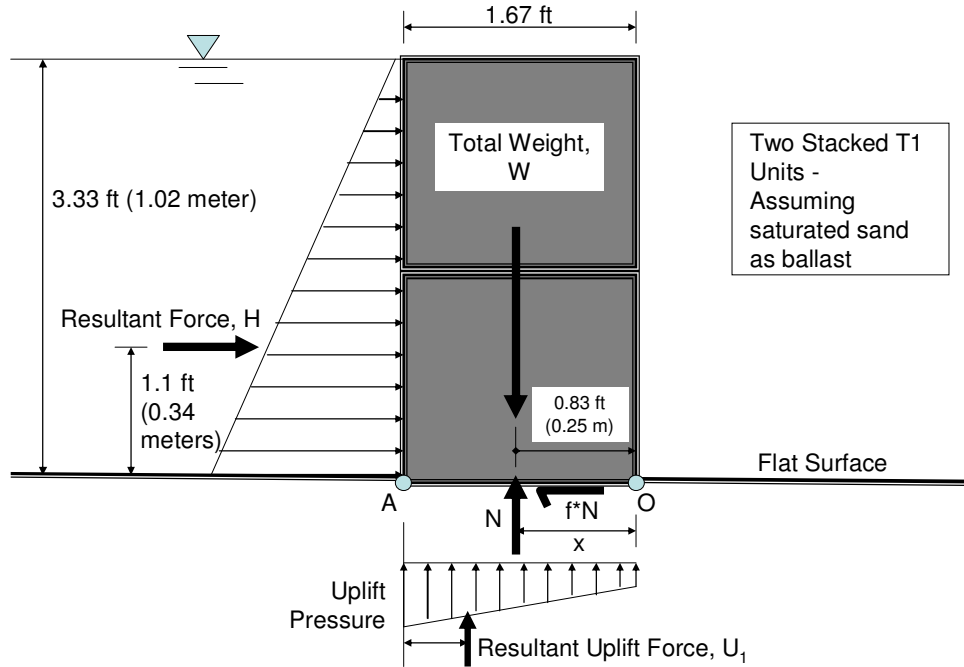


Figure 1.0 – Sand-Filled T1 TYPAR GEOCELLS – Two 0.5-meter Units Stacked Together

$$\text{Total weight of saturated sand inside two T1 units} = 110 \frac{lb_f}{ft^3} * (1.67) * (3.34) = 614 \frac{lb}{ft}$$

$$d_w = \text{distance below headwater} = 3.34 \text{ ft}$$

$$\Delta h = \text{differential head} = 3.34 \text{ ft}$$

$$L_{A-O} = \text{length from point A to point O} = 1.67 \text{ ft}$$

$$L_T = \text{total length from water elevation to point O} = 3.34 + 1.67 = 5 \text{ ft.}$$

$$\text{Uplift pressure at point A} = (d_w - \frac{\Delta h * (d_w)}{L_T}) * (\text{unit weight of water})$$

$$\text{Uplift pressure at point A} = [3.34 \text{ ft} - \frac{3.34 * (3.34)}{(3.34 + 1.67)}] * (62.4 \frac{lb_f}{ft^3}) \cong 69.5 \frac{lb_f}{ft^2}$$

$$\text{Uplift pressure at point O} = (d_w - \frac{\Delta h * (d_w + L_{A-O})}{L_T}) * (\text{unit weight of water})$$

$$\text{Uplift pressure at point O} = [3.34 \text{ ft} - \frac{3.34 * (5)}{(5)}] * (62.4 \frac{lb_f}{ft^3}) \cong 0 \frac{lb_f}{ft^2}$$

Resultant Uplift Force, $U_1 = (0.5 * (69.5) * 1.67 = 58 \frac{lb_f}{ft}$ acting at 1.11 ft from Point O

The resultant force due to hydrostatic pressure, H: $(0.5 * 207.8 * 3.34) = 347 \frac{lb_f}{ft}$

The resultant hydrostatic force, H, is acting at a distance $(\frac{1}{3} * 3.34) = 1.1$ ft up from point A

Resistance to sliding:

Coefficient of friction, f

Normal Force = N

Resulting force acting to resist sliding = $f * N$ (neglecting adhesion)

Summation of Forces:

$$+\uparrow \Sigma F_y = W - N - U_1 = 0;$$

$$614 - N - 58 = 0$$

$$N = 556 \frac{lb_f}{ft}$$

$$+\rightarrow \Sigma F_x = H - f * N = 0;$$

$$347 - f * (556) = 0;$$

f must be ≥ 0.62 for stability against sliding – **Marginal stability based on published interface data**

$$(+\curvearrowright) \Sigma M_o = \text{summation of moments about point O:}$$

$$\text{Overturning Moment (OM)} = 58 * (1.1) + 347 * (1.1)$$

$$\text{Resisting Moment (RM)} = 614 * (0.83)$$

$$\text{Factor of Safety (FS)} = \text{RM/OM} = 510/445.5 = 1.14$$

Solving for FS: FS is less than 1.5- Considered unstable.

Scenario 2: Two stacked sand-filled T2 TYPAR GEOCELLS units:

A free-body diagram of the forces acting on the Scenario 2 arrangement is shown in Figure 2.0 below. The cells are analyzed as a monolithic system.

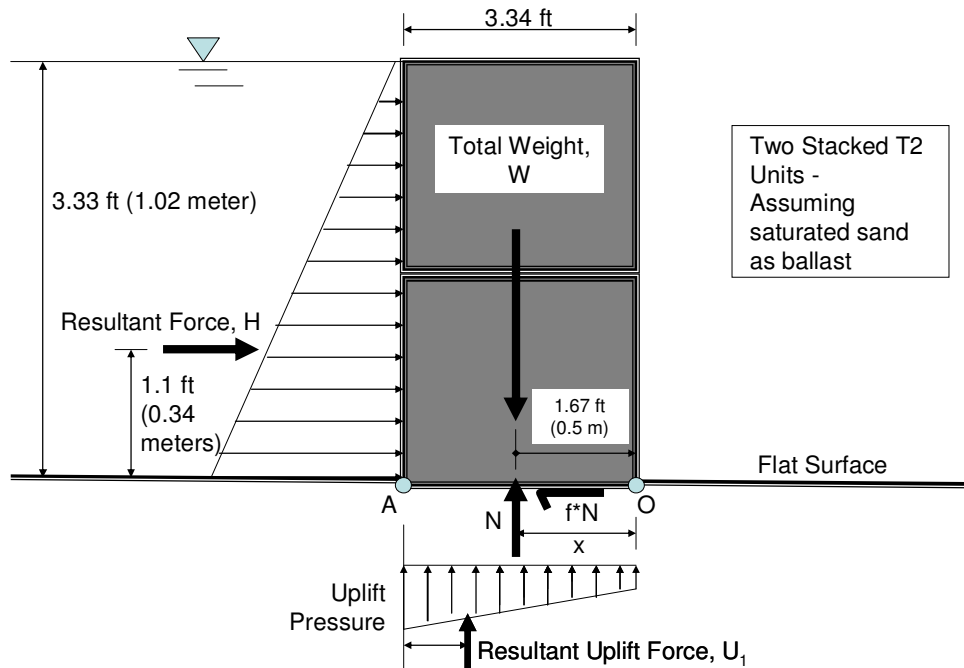


Figure 2.0 – Sand-Filled T2 TYPAR GEOCELLS – Two 0.5-meter Units Stacked Together

$$\text{Total weight of saturated sand inside two T2 units} = 110 \frac{\text{lb}_f}{\text{ft}^3} * (3.34) * (3.34) = 1227.1 \frac{\text{lb}}{\text{ft}}$$

$$d_w = \text{distance below headwater} = 3.34 \text{ ft}$$

$$\Delta h = \text{differential head} = 3.34 \text{ ft}$$

$$L_{A-O} = \text{length from point A to point O} = 3.34 \text{ ft}$$

$$L_T = \text{total length from water elevation to point O} = 3.34 + 3.34 = 6.68 \text{ ft.}$$

$$\text{Uplift pressure at point A} = (d_w - \frac{\Delta h * (d_w)}{L_T}) * (\text{unit weight of water})$$

$$\text{Uplift pressure at point A} = [3.34 \text{ ft} - \frac{3.34 * (3.34)}{(3.34 + 3.34)}] * (62.4 \frac{\text{lb}_f}{\text{ft}^3}) \cong 104.2 \frac{\text{lb}_f}{\text{ft}^2}$$

$$\text{Uplift pressure at point O} = (d_w - \frac{\Delta h * (d_w + L_{A-O})}{L_T}) * (\text{unit weight of water})$$

$$\text{Uplift pressure at point O} = [3.34 \text{ ft} - \frac{3.34 * (6.68)}{(6.68)}] * (62.4 \frac{\text{lb}_f}{\text{ft}^3}) \cong 0 \frac{\text{lb}_f}{\text{ft}^2}$$

Resultant Uplift Force, $U_1 = (0.5 * (104.2) * 3.34 = 174 \frac{lb_f}{ft}$ acting at 2.2 ft from Point O

The resultant force due to hydrostatic pressure, H: $(0.5 * 207.8 * 3.34) = 347 \frac{lb_f}{ft}$

The resultant hydrostatic force, H, is acting at a distance $(\frac{1}{3} * 3.34) = 1.1$ ft up from point A

Resistance to sliding:

Coefficient of friction, f

Normal Force = N

Resulting force acting to resist sliding = $f * N$ (**neglecting adhesion**)

Summation of Forces:

$$+\uparrow \sum F_y = W - N - U_1 = 0;$$

$$1227.1 - N - 174 = 0$$

$$N = 1053.1 \frac{lb_f}{ft}$$

$$+\rightarrow \sum F_x = H - f * N = 0;$$

$$347 - f * (1053.1) = 0;$$

f must be ≥ 0.33 for stability against sliding – stable based on published interface friction coefficients for sand to rock and sand to soil interface conditions (>0.60) and need for safety factors of 1.5 or greater. (SF= 1.8).

$$+\curvearrowright \sum M_o = \text{summation of moments about point O:}$$

$$\text{Overturning Moment (OM)} = 174 * (2.2) + 347 * (1.1)$$

$$\text{Resisting Moment (RM)} = 1227.1 * (1.67)$$

$$\text{Factor of Safety (FS)} = \text{RM/OM} = 2049/765 = 2.67$$

Solving for FS: FS is greater than 1.5- Considered stable.

Scenario 3: One sand-filled T2 TYPAR GEOCELLS unit stacked on top of one sand-filled T3 unit:

A free-body diagram of the forces acting on the Scenario 3 arrangement is shown in Figure 3.0 below. The cells are analyzed as a monolithic system.

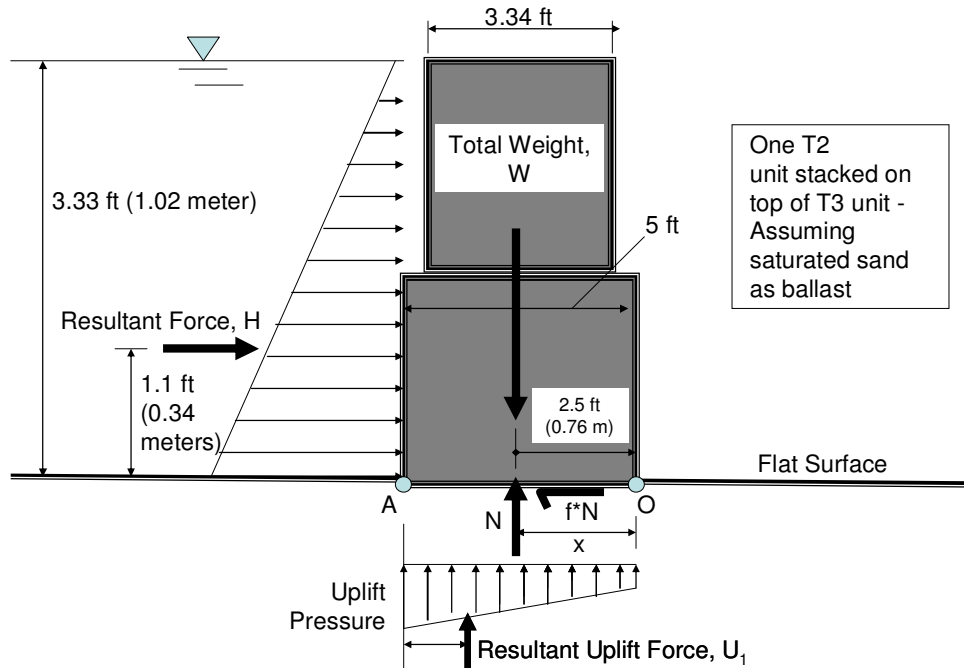


Figure 3.0 – Sand-Filled T2 TYPAR GEOCELLS Stacked Atop T3 TYPAR GEOCELLS Unit

Total weight of saturated sand two units =

$$110 \frac{lb_f}{ft^3} * [(3.34) * (1.67) + (5) * (1.67)] = 1532.1 \frac{lb}{ft}$$

d_w = distance below headwater = 3.34 ft

Δh = differential head = 3.34 ft

L_{A-O} = length from point A to point O = 5.0 ft

L_T = total length from water elevation to point O = 3.34 + 5.0 = 8.34 ft.

$$\text{Uplift pressure at point A} = (d_w - \frac{\Delta h * (d_w)}{L_T}) * (\text{unit weight of water})$$

$$\text{Uplift pressure at point A} = [3.34 \text{ ft} - \frac{3.34 * (3.34)}{(8.34)}] * (62.4 \frac{lb_f}{ft^3}) \cong 125 \frac{lb_f}{ft^2}$$

$$\text{Uplift pressure at point O} = (d_w - \frac{\Delta h * (d_w + L_{A-O})}{L_T}) * (\text{unit weight of water})$$

$$\text{Uplift pressure at point O} = \left[3.34 \text{ ft} - \frac{3.34 * (8.34)}{(8.34)} \right] * \left(62.4 \frac{\text{lb}_f}{\text{ft}^3} \right) \cong 0 \frac{\text{lb}_f}{\text{ft}^2}$$

$$\text{Resultant Uplift Force, } U_1 = (0.5 * (125) * 5.0) = 312.5 \frac{\text{lb}_f}{\text{ft}} \text{ acting at } 3.34 \text{ ft from Point O.}$$

$$\text{The resultant force due to hydrostatic pressure, H: } (0.5 * 207.8 * 3.34) = 347 \frac{\text{lb}_f}{\text{ft}}$$

The resultant hydrostatic force, H, is acting at a distance $\left(\frac{1}{3} * 3.34\right) = 1.1 \text{ ft}$ up from point A

Resistance to sliding:

Coefficient of friction, f

Normal Force = N

Resulting force acting to resist sliding = f*N (neglecting adhesion)

Summation of Forces:

$$+\uparrow \sum F_y = W - N - U_1 = 0;$$

$$1532.1 - N - 312.5 = 0$$

$$N = 1219.6 \frac{\text{lb}_f}{\text{ft}}$$

$$+\rightarrow \sum F_x = H - f*N = 0;$$

$$347 - f*(1219.6) = 0;$$

f must be ≥ 0.28 for stability against sliding – provides satisfactory stability based on published interface friction coefficients for sand to rock and sand to soil interface conditions (>0.6) with a safety factor of 2.1.

$$+\curvearrowright \sum M_o = \text{summation of moments about point O:}$$

$$\text{Overturning Moment (OM)} = 312.5*(3.34) + 347*(1.1)$$

$$\text{Resisting Moment (RM)} = 1532.1*(2.5)$$

$$\text{Factor of Safety (FS)} = \text{RM/OM} = 3830/1425 = 2.68$$

Solving for FS: FS is greater than 1.5- Considered stable.

Scenario 4: Two sand-filled T3 TYPAR GEOCELLS units stacked on top of each other:

A free-body diagram of the forces acting on the Scenario 4 arrangement is shown in Figure 4.0 below. The cells are analyzed as a monolithic system.

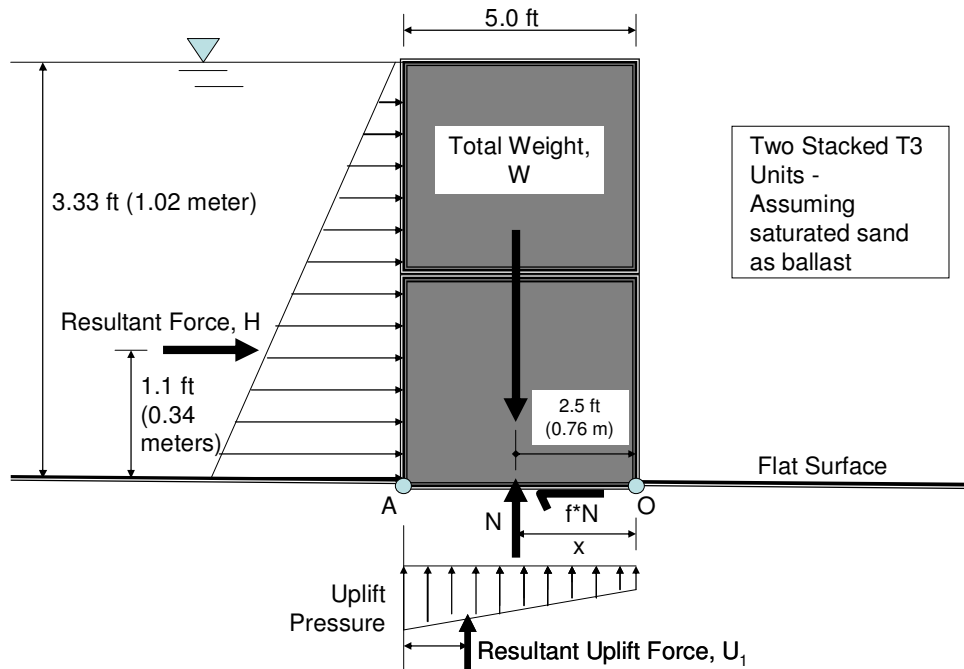


Figure 4.0 – Two Sand-Filled T3 TYPAR GEOCELLS Units Stacked Atop One Another

$$\text{Total weight of saturated sand two units} = 110 \frac{lb_f}{ft^3} * [(5) * (3.34)] = 1837 \frac{lb_f}{ft}$$

$$d_w = \text{distance below headwater} = 3.34 \text{ ft}$$

$$\Delta h = \text{differential head} = 3.34 \text{ ft}$$

$$L_{A-O} = \text{length from point A to point O} = 5.0 \text{ ft}$$

$$L_T = \text{total length from water elevation to point O} = 3.34 + 5.0 = 8.34 \text{ ft.}$$

$$\text{Uplift pressure at point A} = (d_w - \frac{\Delta h * (d_w)}{L_T}) * (\text{unit weight of water})$$

$$\text{Uplift pressure at point A} = [3.34 \text{ ft} - \frac{3.34 * (3.34)}{(8.34)}] * (62.4 \frac{lb_f}{ft^3}) \cong 125 \frac{lb_f}{ft^2}$$

$$\text{Uplift pressure at point O} = (d_w - \frac{\Delta h * (d_w + L_{A-O})}{L_T}) * (\text{unit weight of water})$$

$$\text{Uplift pressure at point O} = [3.34 \text{ ft} - \frac{3.34 * (8.34)}{(8.34)}] * (62.4 \frac{\text{lb}_f}{\text{ft}^3}) \cong 0 \frac{\text{lb}_f}{\text{ft}^2}$$

$$\text{Resultant Uplift Force, } U_1 = (0.5 * (125) * 5.0) = 312.5 \frac{\text{lb}_f}{\text{ft}} \text{ acting at 3.34 ft from Point O.}$$

$$\text{The resultant force due to hydrostatic pressure, H: } (0.5 * 207.8 * 3.34) = 347 \frac{\text{lb}_f}{\text{ft}}$$

The resultant hydrostatic force, H, is acting at a distance $(\frac{1}{3} * 3.34) = 1.1 \text{ ft}$ up from point A

Resistance to sliding:

Coefficient of friction, f

Normal Force = N

Resulting force acting to resist sliding = f*N (neglecting adhesion)

Summation of Forces:

$$+\uparrow \sum F_y = W - N - U_1 = 0;$$

$$1837 - N - 312.5 = 0$$

$$N = 1524.5 \frac{\text{lb}_f}{\text{ft}}$$

$$+\rightarrow \sum F_x = H - f*N = 0;$$

$$347 - f*(1524.5) = 0;$$

f must be ≥ 0.23 for stability against sliding – provides satisfactory stability based on published interface friction coefficients for sand to rock and sand to soil interface conditions (>0.6) with a safety factor of 2.6.

$$+\curvearrowright \sum M_o = \text{summation of moments about point O:}$$

$$\text{Overturning Moment (OM)} = 312.5*(3.34) + 347*(1.1)$$

$$\text{Resisting Moment (RM)} = 1837*(2.5)$$

Factor of Safety (FS) = $RM/OM = 4593/1425 = 3.22$

Solving for FS: FS is greater than 1.5- **Considered stable.**

Scenario 5: Three (3) sand-filled T3 TYPAR GEOCELLS units stacked on top of each other:

A free-body diagram of the forces acting on the Scenario 5 arrangement is shown in Figure 5.0 below. The cells are analyzed as a monolithic system.

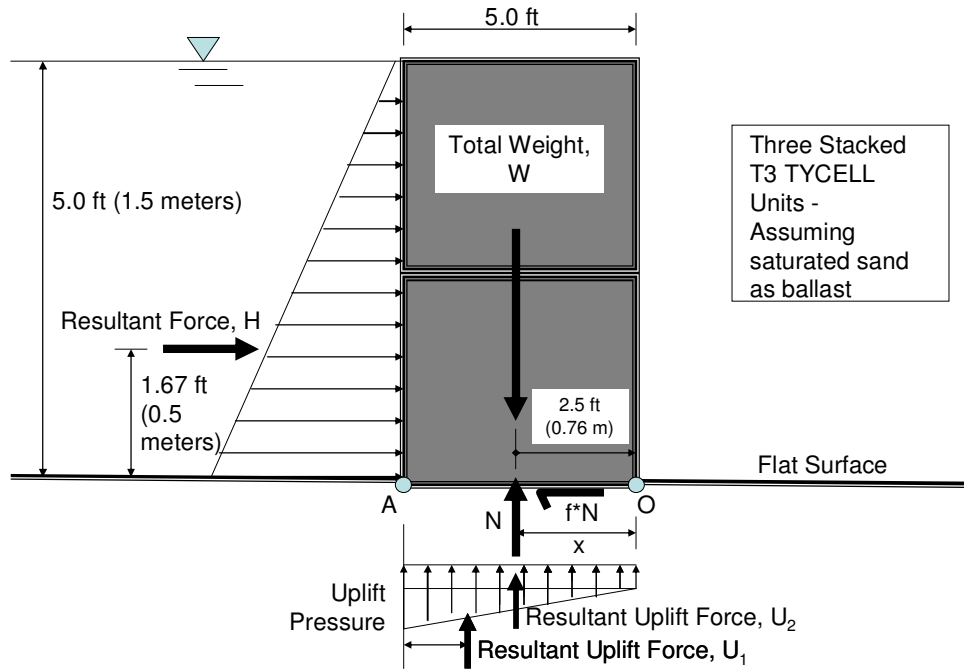


Figure 5.0 – Three (3) Sand-Filled T3 TYPAR GEOCELLS Units Stacked Atop One Another

$$\text{Total weight of saturated sand three units} = 110 \frac{lb_f}{ft^3} * [(5) * (5)] = 2750 \frac{lb}{ft}$$

$$d_w = \text{distance below headwater} = 5.0 \text{ ft}$$

$$\Delta h = \text{differential head} = 5.0 \text{ ft}$$

$$L_{A-O} = \text{length from point A to point O} = 5.0 \text{ ft}$$

$$L_T = \text{total length from water elevation to point O} = 5.0 + 5.0 = 10.0 \text{ ft.}$$

$$\text{Uplift pressure at point A} = (d_w - \frac{\Delta h * (d_w)}{L_T}) * (\text{unit weight of water})$$

$$\text{Uplift pressure at point A} = [5.0 \text{ ft} - \frac{5.0 * (5.0)}{(10)}] * (62.4 \frac{lb_f}{ft^3}) \cong 156 \frac{lb_f}{ft^2}$$

$$\text{Uplift pressure at point O} = (d_w - \frac{\Delta h * (d_w + L_{A-O})}{L_T}) * (\text{unit weight of water})$$

$$\text{Uplift pressure at point O} = \left[5.0 \text{ ft} - \frac{5.0 * (10)}{(10)} \right] * \left(62.4 \frac{\text{lb}_f}{\text{ft}^3} \right) \cong 0 \frac{\text{lb}_f}{\text{ft}^2}$$

$$\text{Resultant Uplift Force, } U_1 = (0.5 * (156) * 5.0) = 390 \frac{\text{lb}_f}{\text{ft}} \text{ acting at 3.34 ft from Point O.}$$

$$\text{The resultant force due to hydrostatic pressure, H: } (0.5 * 312 * 5.0) = 780 \frac{\text{lb}_f}{\text{ft}}$$

The resultant hydrostatic force, H, is acting at a distance $\left(\frac{1}{3} * 5.0 \right) = 1.67 \text{ ft}$ up from point

A

Resistance to sliding:

Coefficient of friction, f

Normal Force = N

Resulting force acting to resist sliding = f*N (neglecting adhesion)

Summation of Forces:

$$+\uparrow \Sigma F_y = W - N - U_1 = 0;$$

$$2750 - N - 390 = 0$$

$$N = 2360 \frac{\text{lb}_f}{\text{ft}}$$

$$+\rightarrow \Sigma F_x = H - f*N = 0;$$

$$780 - f*(2360) = 0;$$

f must be ≥ 0.33 for stability against sliding – provides satisfactory stability based on published interface friction coefficients for sand to rock and sand to soil interface conditions (>0.6) with a safety factor of 1.8.

$$(+\curvearrowright) \Sigma M_o = \text{summation of moments about point O:}$$

$$\text{Overturning Moment (OM)} = 390*(3.34) + 780*(1.67)$$

$$\text{Resisting Moment (RM)} = 2750*(2.5)$$

Factor of Safety (FS) = RM/OM = 6875/2605= 2.63

Solving for FS: FS is greater than 1.5- **Considered stable.**

Scenario 6: Four (4) sand-filled T4 TYPAR GEOCELLS units stacked on top of each other:

A free-body diagram of the forces acting on the Scenario 6 arrangement is shown in Figure 6.0 below. The cells are analyzed as a monolithic system.

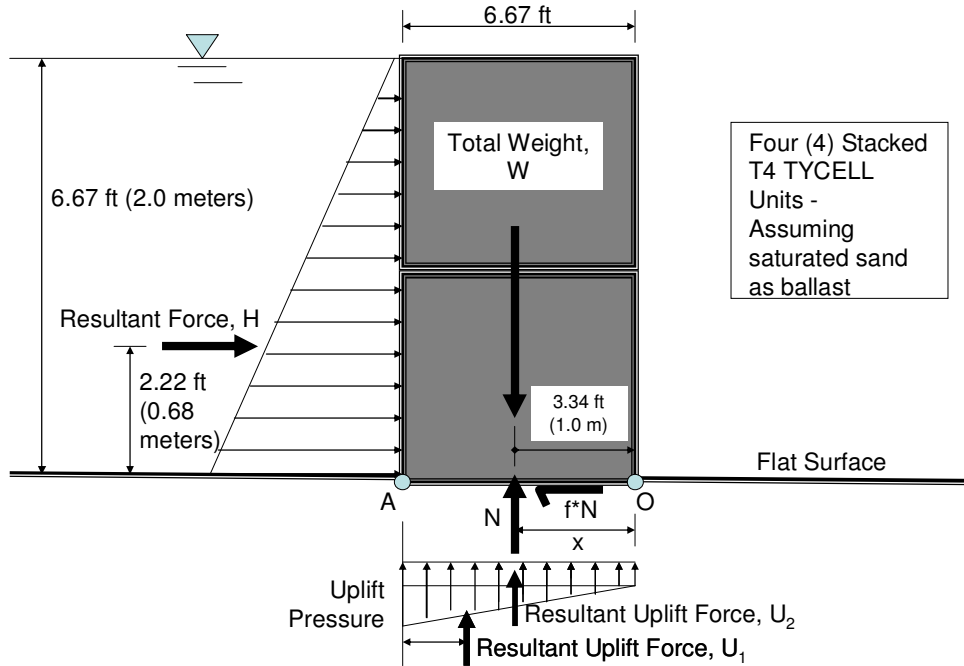


Figure 6.0 – Four (4) Sand-Filled T4 TYPAR GEOCELLS Units Stacked Atop One Another

$$\text{Total weight of saturated sand three units} = 110 \frac{lb_f}{ft^3} * [(6.67) * (6.67)] = 4894 \frac{lb}{ft}$$

$$d_w = \text{distance below headwater} = 6.67 \text{ ft}$$

$$\Delta h = \text{differential head} = 6.67 \text{ ft}$$

$$L_{A-O} = \text{length from point A to point O} = 6.67 \text{ ft}$$

$$L_T = \text{total length from water elevation to point O} = 6.67 + 6.67 = 13.34 \text{ ft.}$$

$$\text{Uplift pressure at point A} = (d_w - \frac{\Delta h * (d_w)}{L_T}) * (\text{unit weight of water})$$

$$\text{Uplift pressure at point A} = [6.67 \text{ ft} - \frac{6.67 * (6.67)}{(13.34)}] * (62.4 \frac{lb_f}{ft^3}) \cong 208.1 \frac{lb_f}{ft^2}$$

$$\text{Uplift pressure at point O} = (d_w - \frac{\Delta h * (d_w + L_{A-O})}{L_T}) * (\text{unit weight of water})$$

$$\text{Uplift pressure at point O} = [6.67 \text{ ft} - \frac{6.67 * (13.34)}{(13.34)}] * (62.4 \frac{\text{lb}_f}{\text{ft}^3}) \cong 0 \frac{\text{lb}_f}{\text{ft}^2}$$

$$\text{Resultant Uplift Force, } U_1 = (0.5 * (208.1) * 6.67) = 694 \frac{\text{lb}_f}{\text{ft}} \text{ acting at 4.45 ft from Point O.}$$

$$\text{The resultant force due to hydrostatic pressure, H: } (0.5 * 416.21 * 6.67) = 1388.1 \frac{\text{lb}_f}{\text{ft}}$$

The resultant hydrostatic force, H, is acting at a distance $(\frac{1}{3} * 6.67) = 2.22 \text{ ft}$ up from point A

Resistance to sliding:

Coefficient of friction, f

Normal Force = N

Resulting force acting to resist sliding = f*N (neglecting adhesion)

Summation of Forces:

$$+\uparrow \sum F_y = W - N - U_1 = 0;$$

$$4894 - N - 694 = 0$$

$$N = 4200 \frac{\text{lb}_f}{\text{ft}}$$

$$+\rightarrow \sum F_x = H - f*N = 0;$$

$$1388.1 - f*(4200) = 0;$$

f must be ≥ 0.33 for stability against sliding – **provides satisfactory stability based on published interface friction coefficients for sand to rock and sand to soil interface conditions (>0.6) with a safety factor of 1.8.**

$$\curvearrowright + \sum M_o = \text{summation of moments about point O:}$$

$$694*(4.45) + 1388.1*(2.22) - 4894*(3.34) + 4200*(x) = 0$$

Overturing Moment (OM) = $694 \cdot (4.45) + 1388 \cdot (2.22)$
Resisting Moment (RM) = $4894 \cdot (3.34)$

Factor of Safety (FS) = $RM/OM = 16,346/6170 = 2.65$

Solving for FS: FS is greater than 1.5- **Considered stable.**